



Cosmological inference from self-consistent Bayesian forward modelling of deep galaxy redshift surveys

Doogesh Kodi Ramanah

Guilhem Lavaux
Jens Jasche
Ben Wandelt

Institut d'Astrophysique de Paris

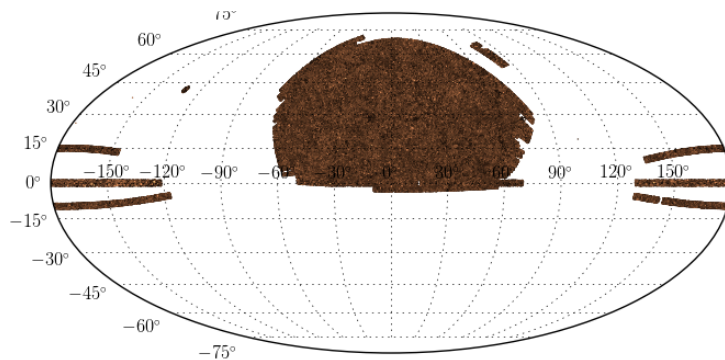
Statistical challenges for large-scale structure in the era of LSST, Oxford, 2018



Cosmological data challenges

- Incomplete noisy sky with systematic effects (masks, complex noise models, ...)
- **Transformation:** physical (comoving) space \longleftrightarrow observational space

Noisy large-scale structure data



signal
reconstruction

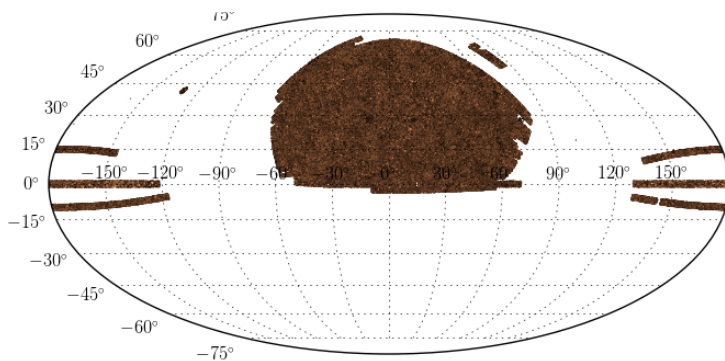


Cosmology encoded in expansion & global geometry (Alcock-Paczyński effect)

Cosmological data challenges

- Incomplete noisy sky with systematic effects (masks, complex noise models, ...)
- **Transformation:** physical (comoving) space \longleftrightarrow observational space

Noisy large-scale structure data



Credit: Assassin's Creed (Ubisoft)

AQUILA Consortium

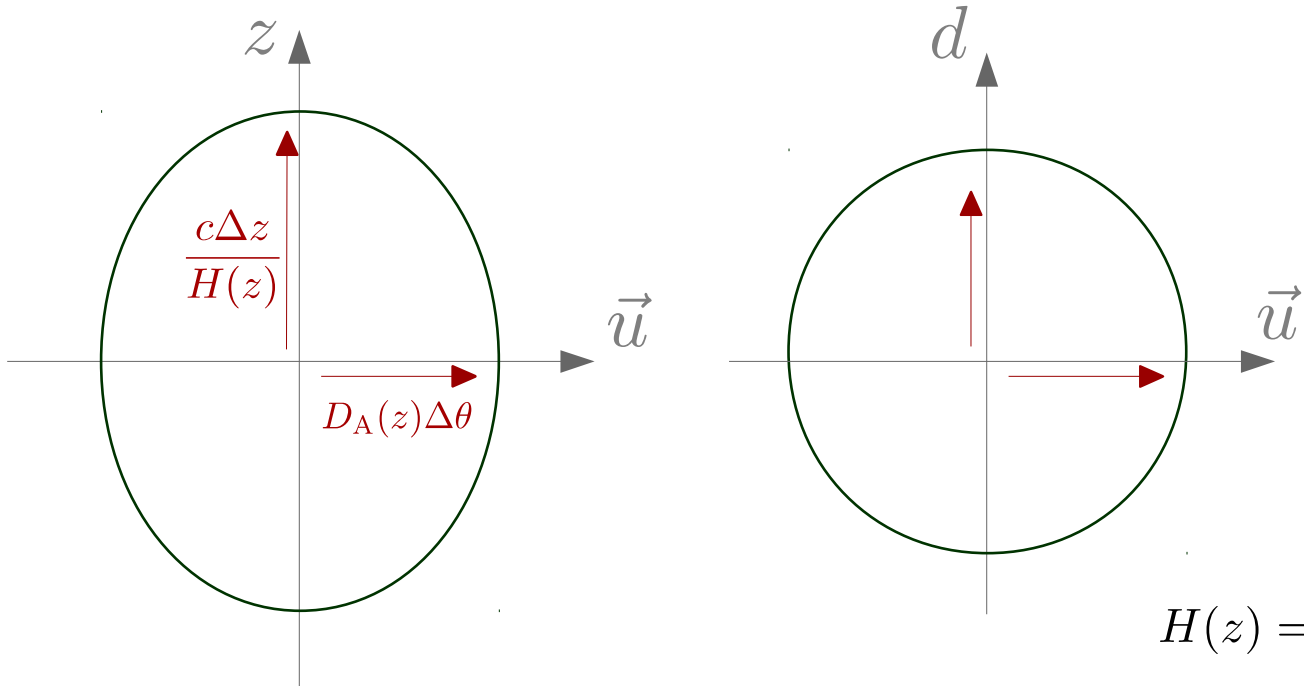
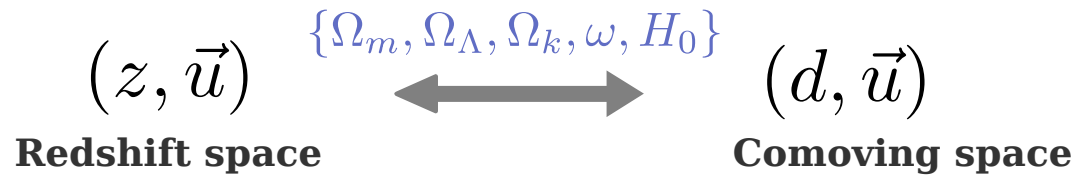
HADES \longrightarrow BORG \longrightarrow ALTAIR

★ **ALTAIR** (ALcock-Paczyński consTRAIned Reconstruction) (DKR, Lavaux & Wandelt 2018, in prep.)

- Liberate cosmology \rightarrow Cosmological parameter inference via the **Alcock-Paczyński (AP)** test
- Also jointly infer underlying **3D power spectrum** + more realistic (**non-linear**) **bias** model

Alcock-Paczyński Test

Coordinate Transformation



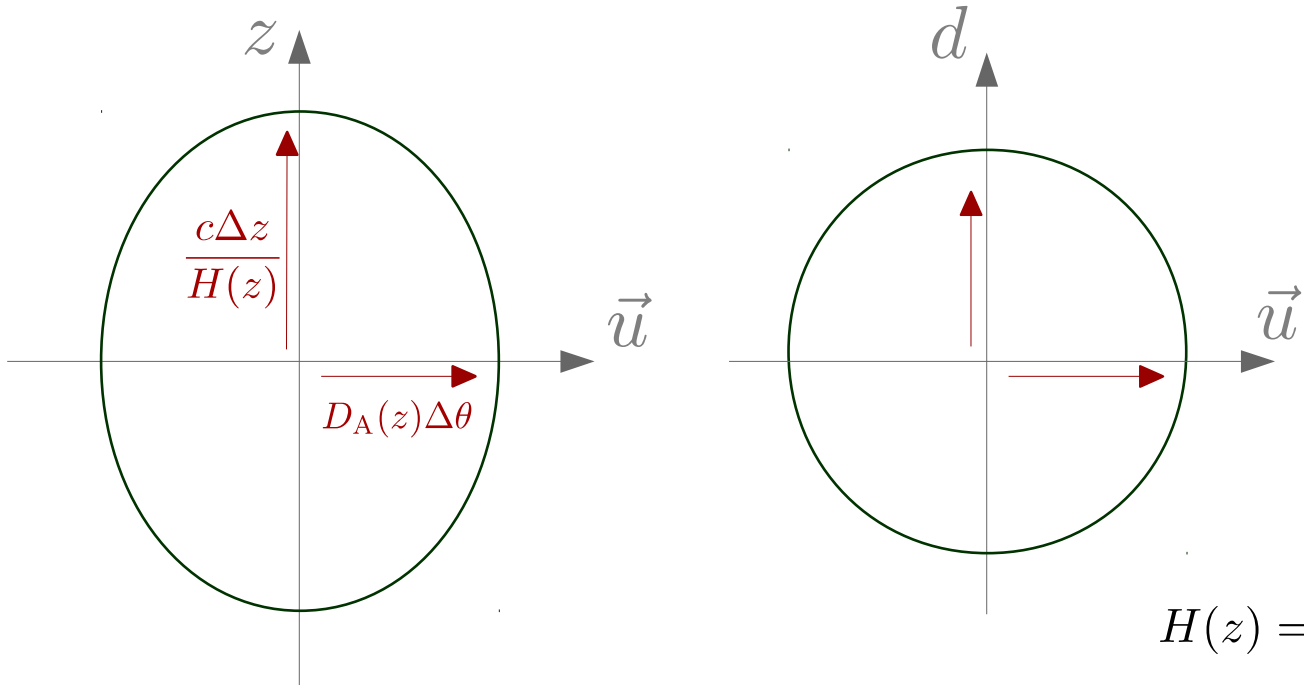
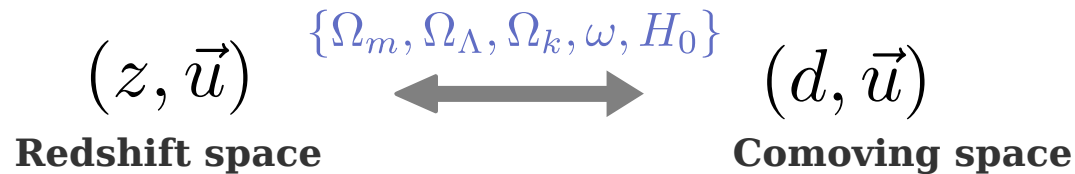
$$d = \int_{z_1}^{z_2} \frac{1}{cH(z)}$$

$$H(z) = H_0(\Omega_m(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda)^{\frac{1}{2}}$$

- Test of the expansion & geometry of the Universe
- No dependence on evolution of galaxies but only on geometry of Universe

Alcock-Paczyński Test

Coordinate Transformation



- Distortions due to assumption of incorrect cosmological parameters
- Structure: **Spherical** → **Ellipsoidal**
- Statistical distribution: **Isotropic** → **Anisotropic**

$$d = \int_{z_1}^{z_2} \frac{1}{cH(z)}$$

$$H(z) = H_0(\Omega_m(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda)^{\frac{1}{2}}$$

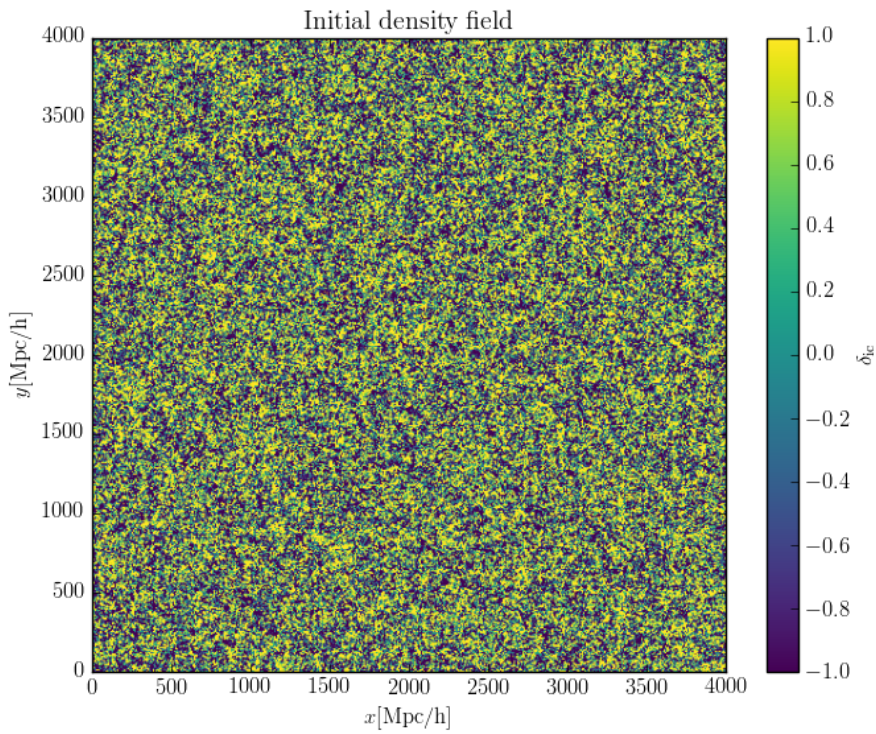
- Test of the expansion & geometry of the Universe
- No dependence on evolution of galaxies but only on geometry of Universe

Visualising cosmic expansion

[Standard Λ CDM]

- $\{\Omega_m = 0.3089, \Omega_\Lambda = 0.6911, \Omega_k = 0, \omega = -1, h = 0.6774\}$

Initial conditions

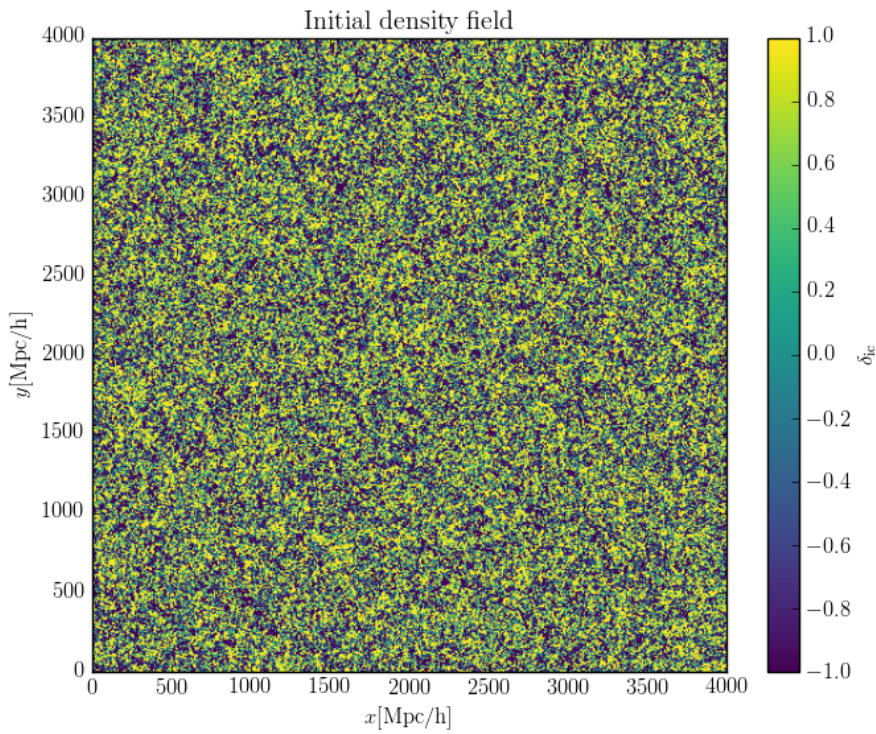


Visualising cosmic expansion

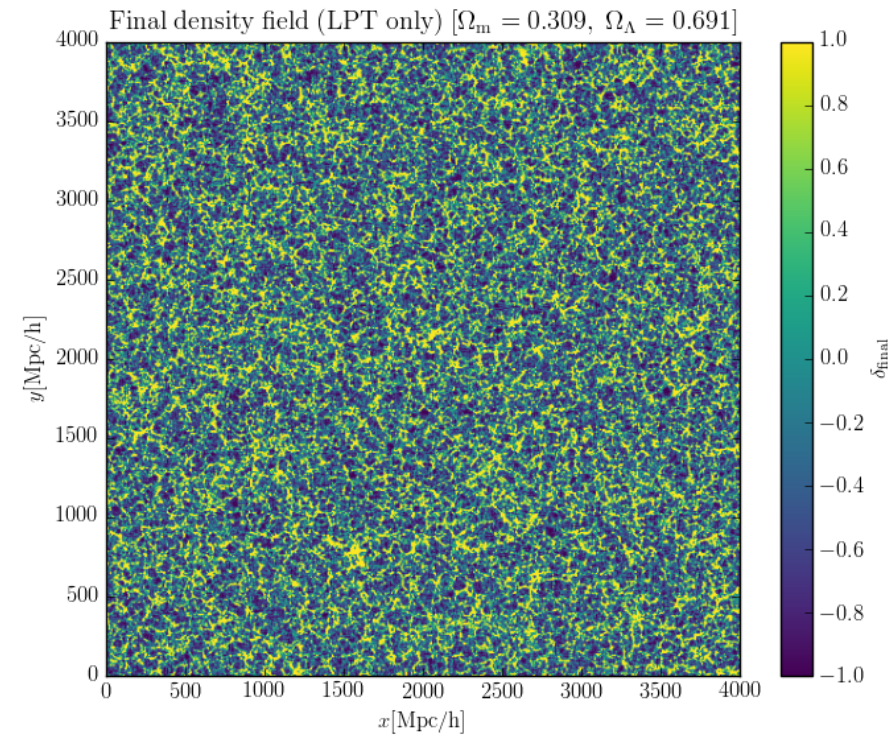
[Standard Λ CDM]

- $\{\Omega_m = 0.3089, \Omega_\Lambda = 0.6911, \Omega_k = 0, \omega = -1, h = 0.6774\}$

Initial conditions



Final (LPT) density field



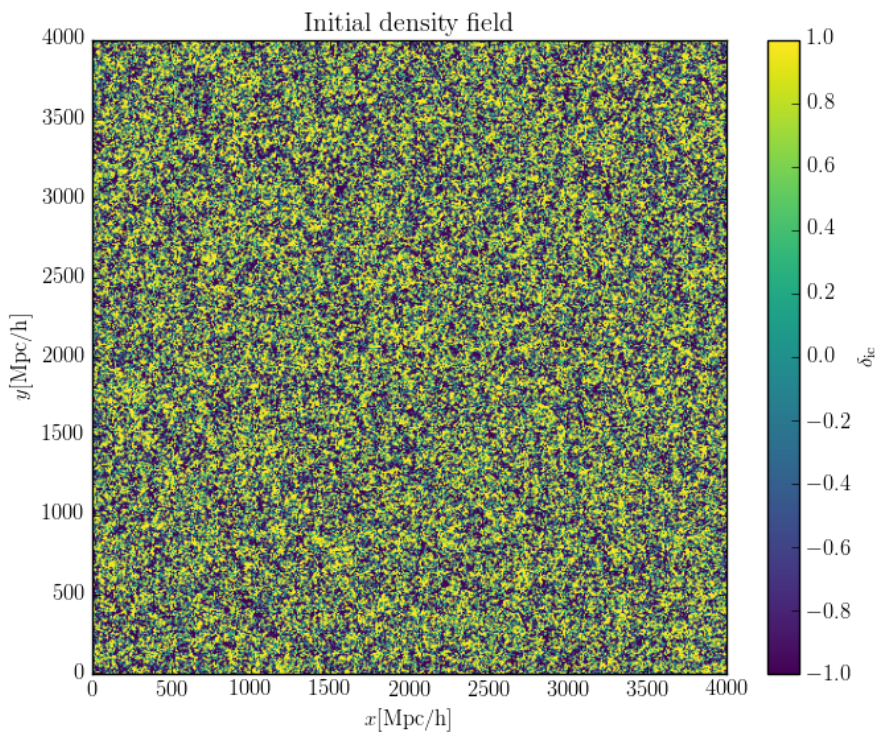
Comoving space

Visualising cosmic expansion

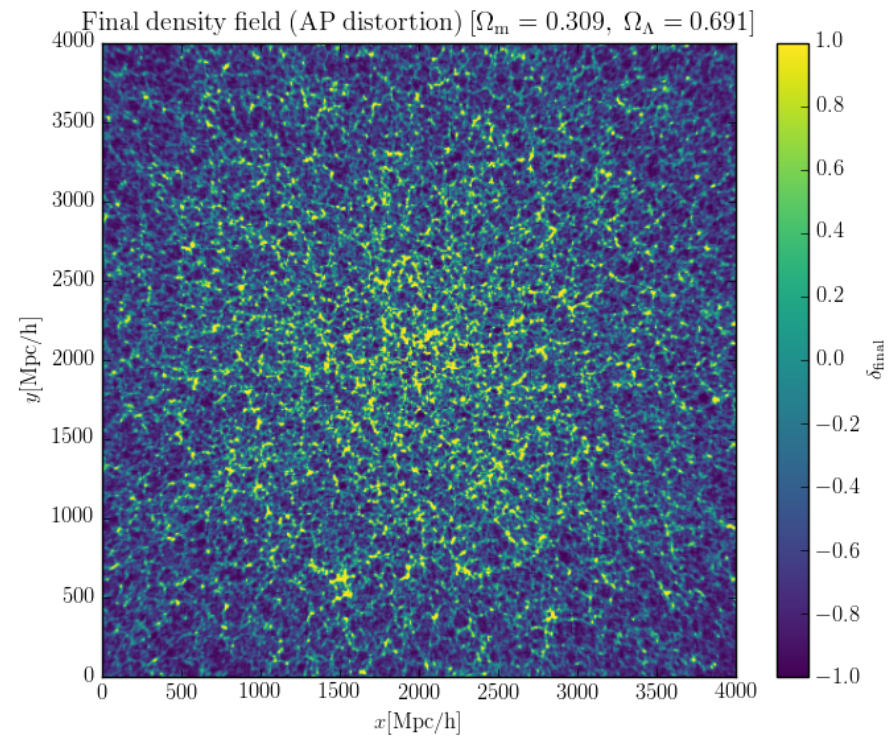
[Standard Λ CDM]

- $\{\Omega_m = 0.3089, \Omega_\Lambda = 0.6911, \Omega_k = 0, \omega = -1, h = 0.6774\}$

Initial conditions



Final (LPT+AP) density field



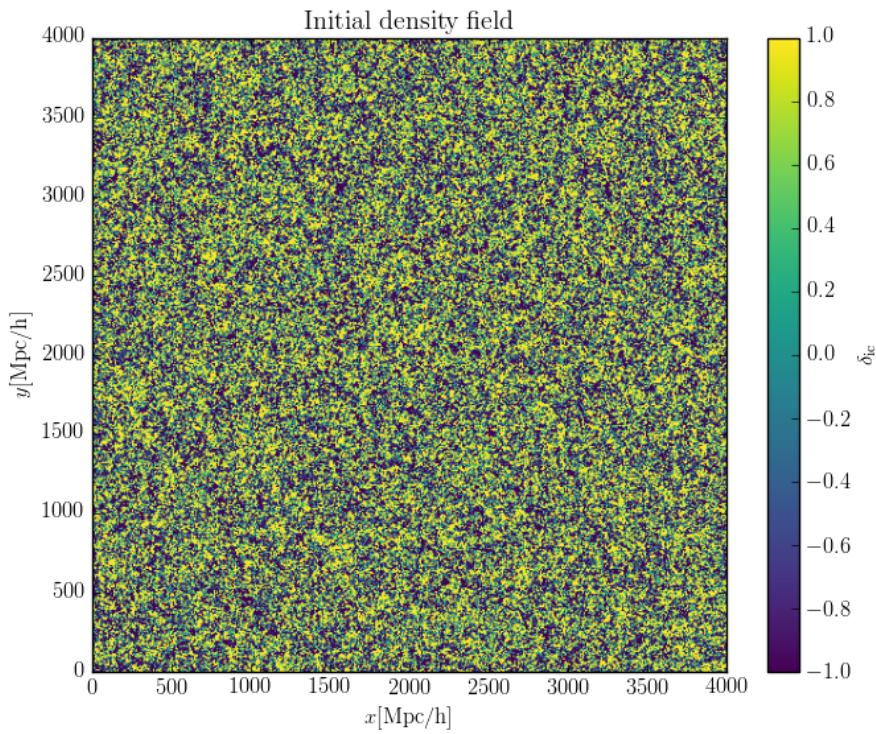
Redshift space

Visualising cosmic expansion

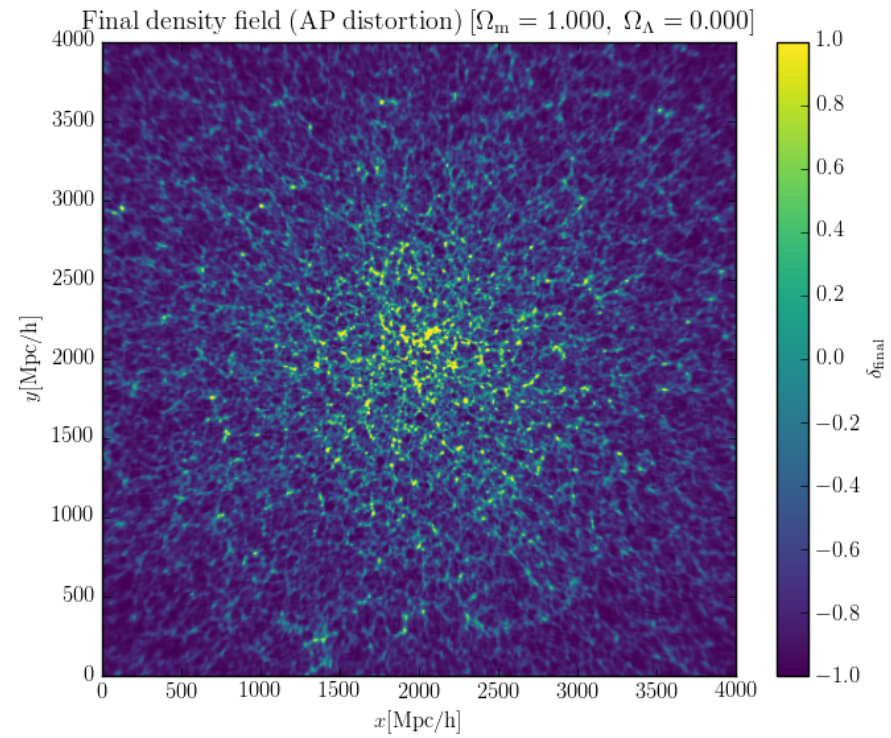
[Einstein-de Sitter Universe]

- $\{\Omega_m = 1.0, \Omega_\Lambda = 0, \Omega_k = 0, \omega = -1, h = 0.6774\}$

Initial conditions

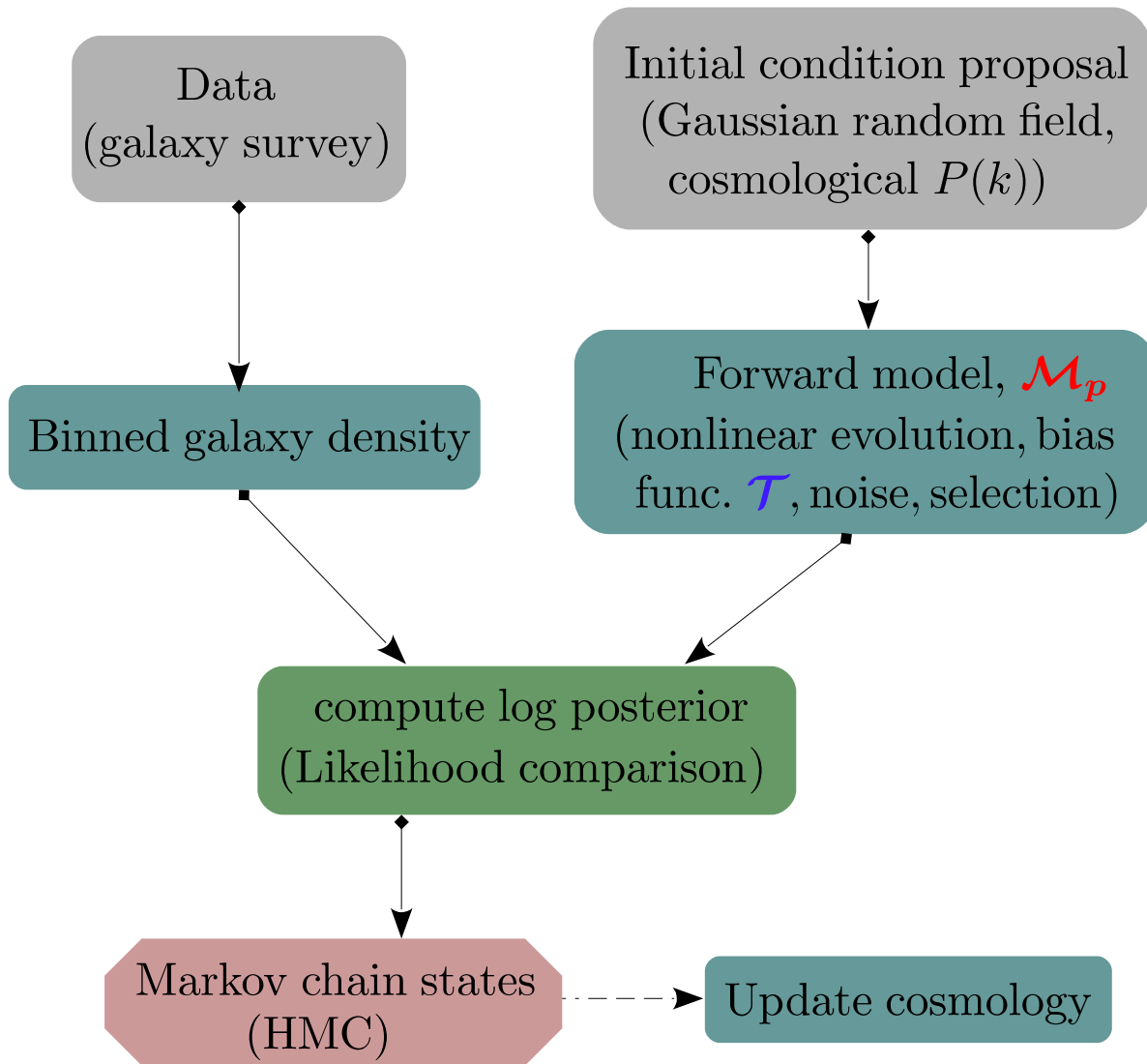


Final (LPT+AP) density field



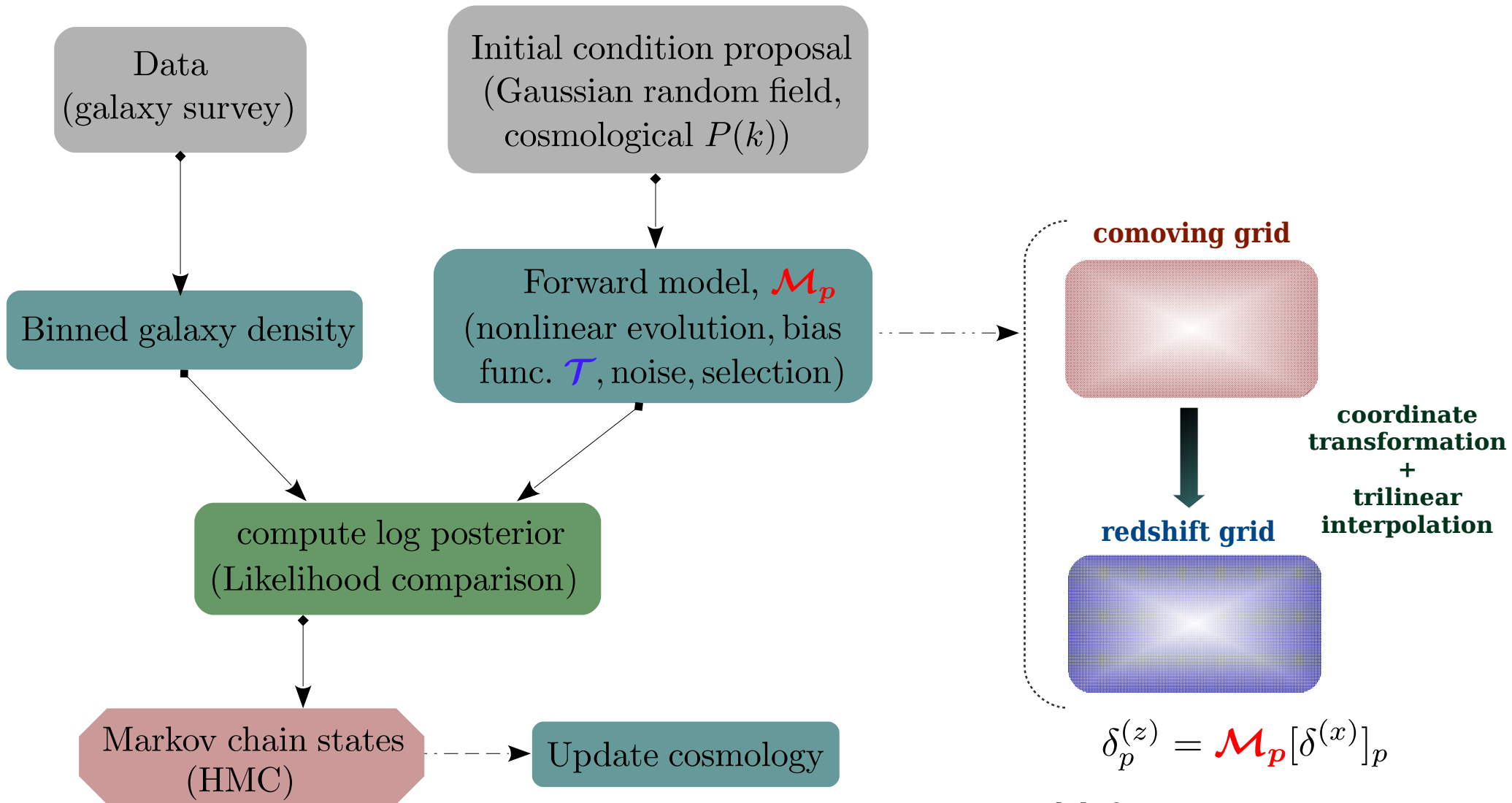
Redshift space

ALTAIR reconstruction scheme



Data model:
$$N_p^g = R(z_p) \bar{N}_p^g \mathcal{T} (1 + \mathcal{M}_p \{ [\hat{\delta}_k]_{\tilde{p}} \}_p)$$

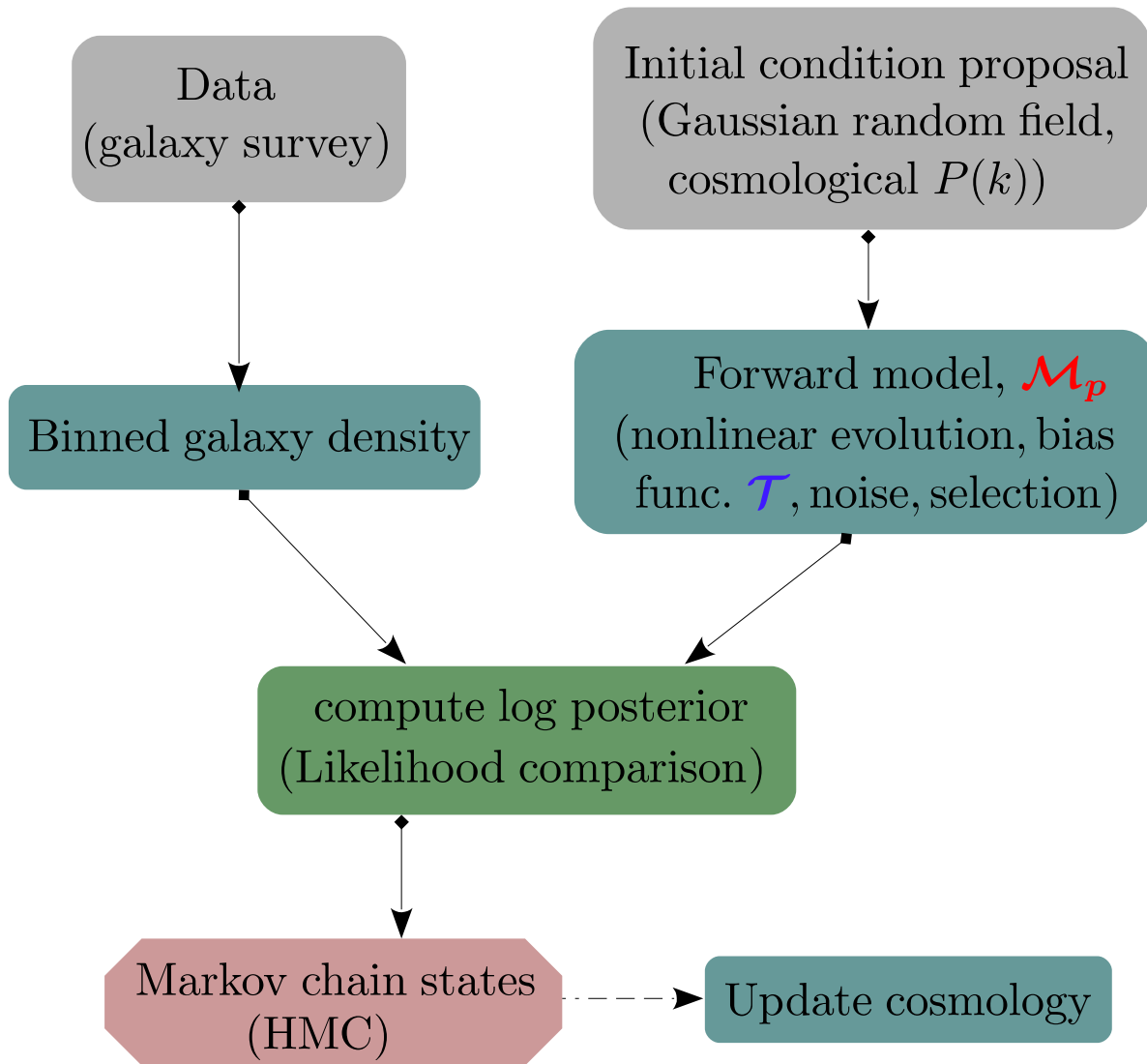
ALTAIR reconstruction scheme



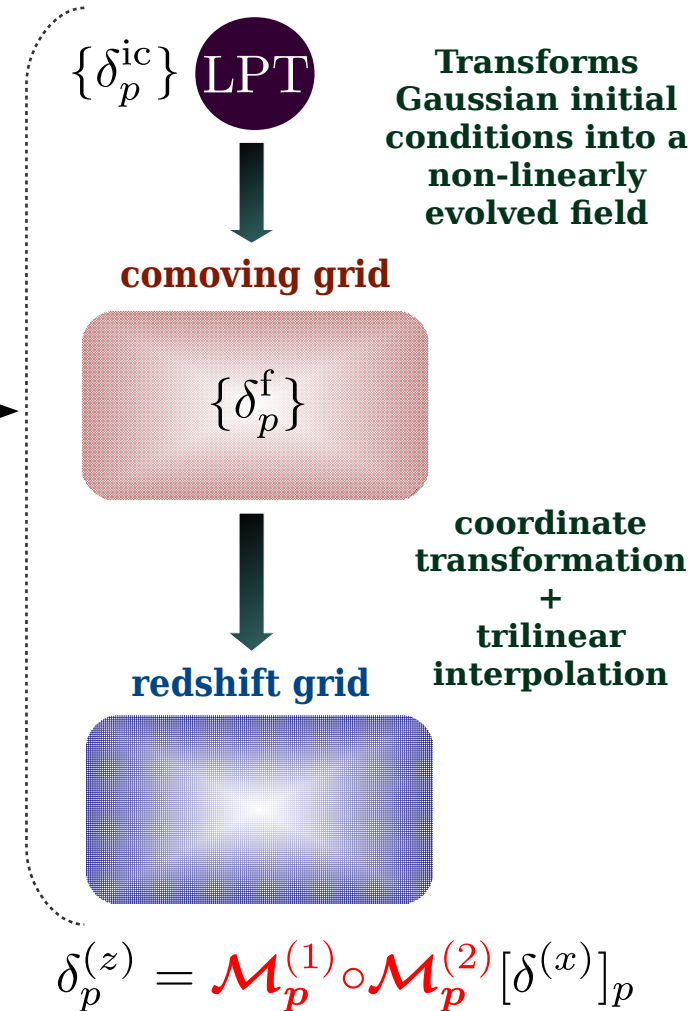
- Redshift space representation allows comparison with data via likelihood

Data model: $N_p^g = R(z_p) \bar{N}_p^g \mathcal{T} (1 + \mathcal{M}_p \{ [\hat{\delta}_k]_{\tilde{p}} \}_p)$

ALTAIR reconstruction scheme



Lagrangian Perturbation Theory



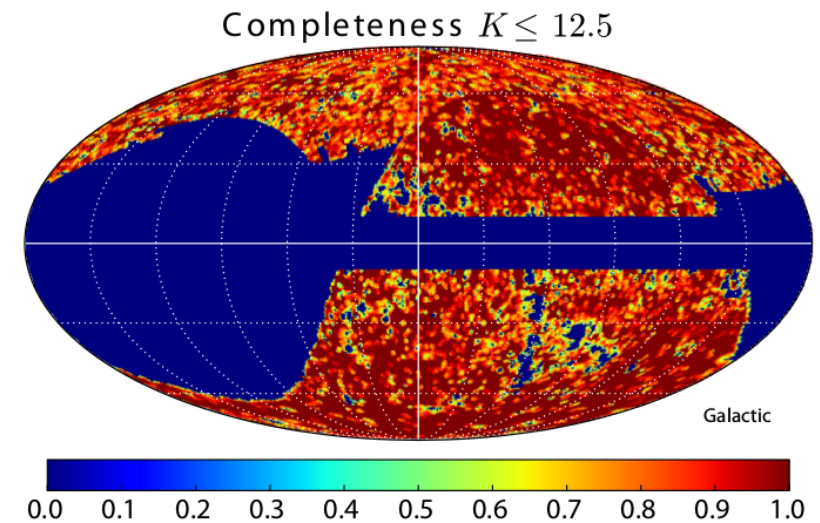
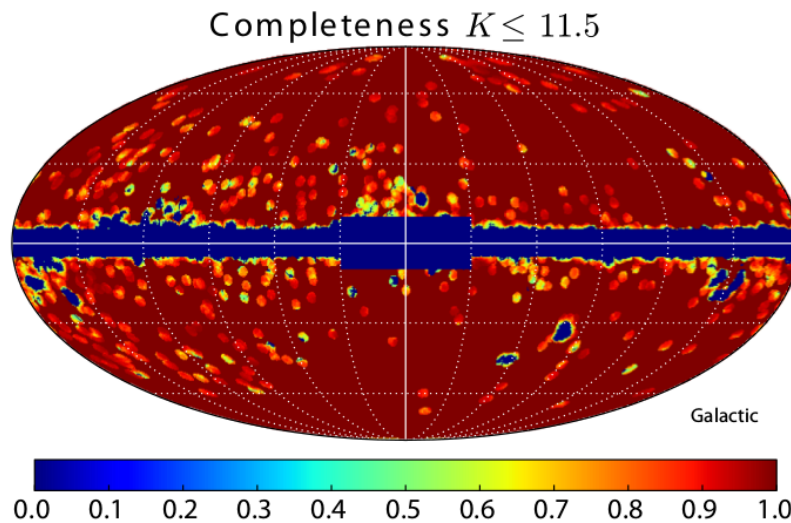
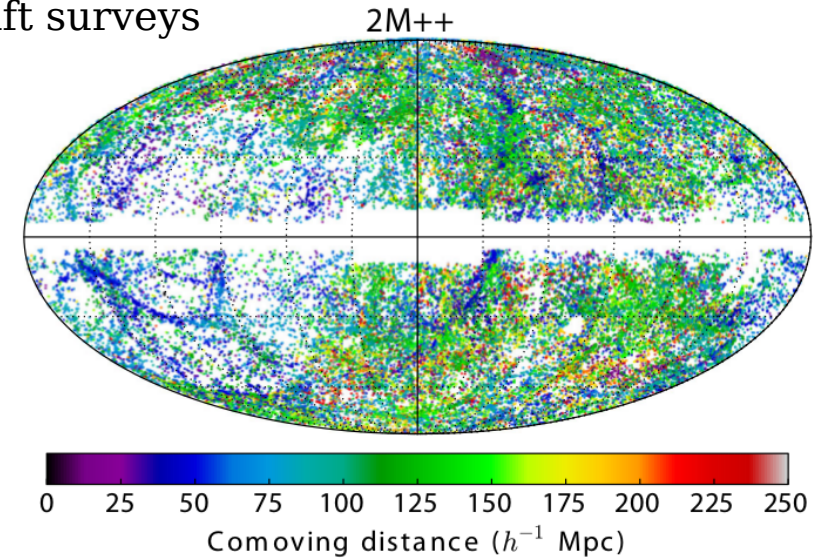
- Redshift space representation allows comparison with data via likelihood

Data model: $N_p^g = R(z_p) \bar{N}_p^g \mathcal{T} (1 + \mathcal{M}_p \{[\hat{\delta}_k]_{\tilde{p}}\}_p)$

Validation on mock catalogues (A) - 2M++

2M++ galaxy compilation : (Lavaux & Hudson 2011)

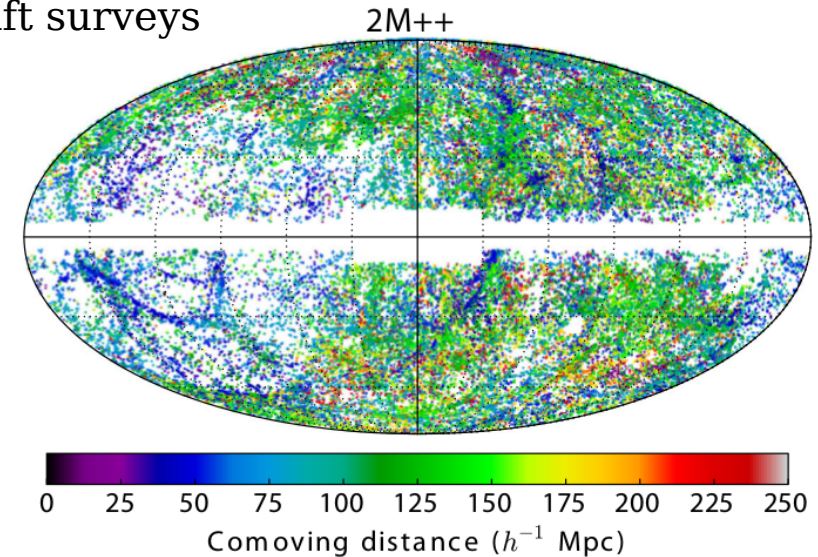
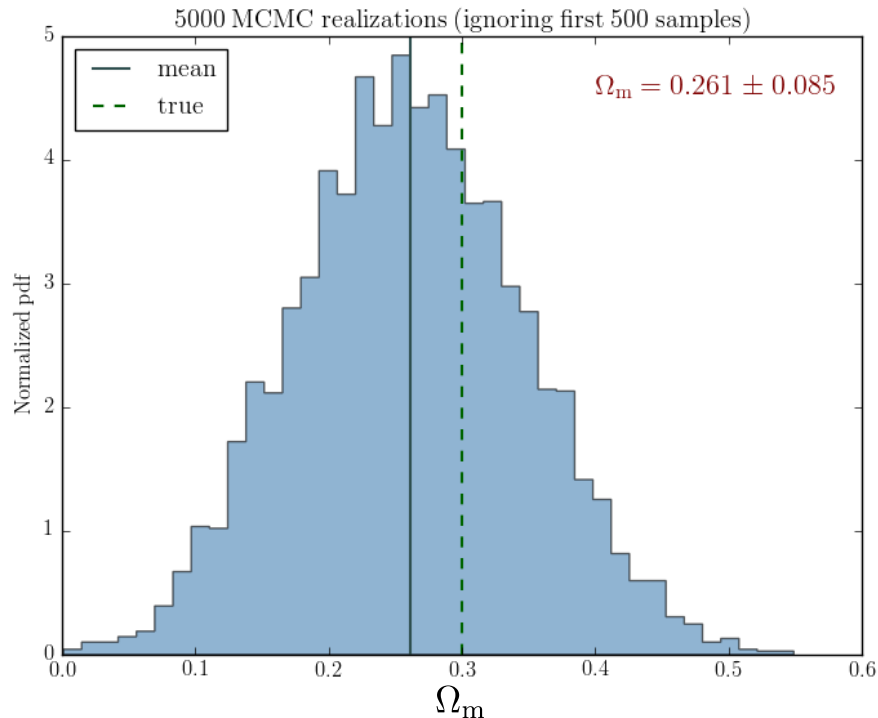
- Superset of {**2MASS**, **SDSS-DR7**, **6dFGS-DR3**} redshift surveys
- Greater depth & higher sampling than **IRAS** survey
- Sub-divided into 2 *K*-bands
- Anisotropic selection and strong galaxy clustering



Validation on mock catalogues (A) - 2M++

2M++ galaxy compilation : (Lavaux & Hudson 2011)

- Superset of {**2MASS**, **SDSS-DR7**, **6dFGS-DR3**} redshift surveys
- Greater depth & higher sampling than **IRAS** survey
- Sub-divided into 2 *K*-bands
- Anisotropic selection and strong galaxy clustering



Simulation box

Grid with 32^3 voxels
1200 Mpc side length

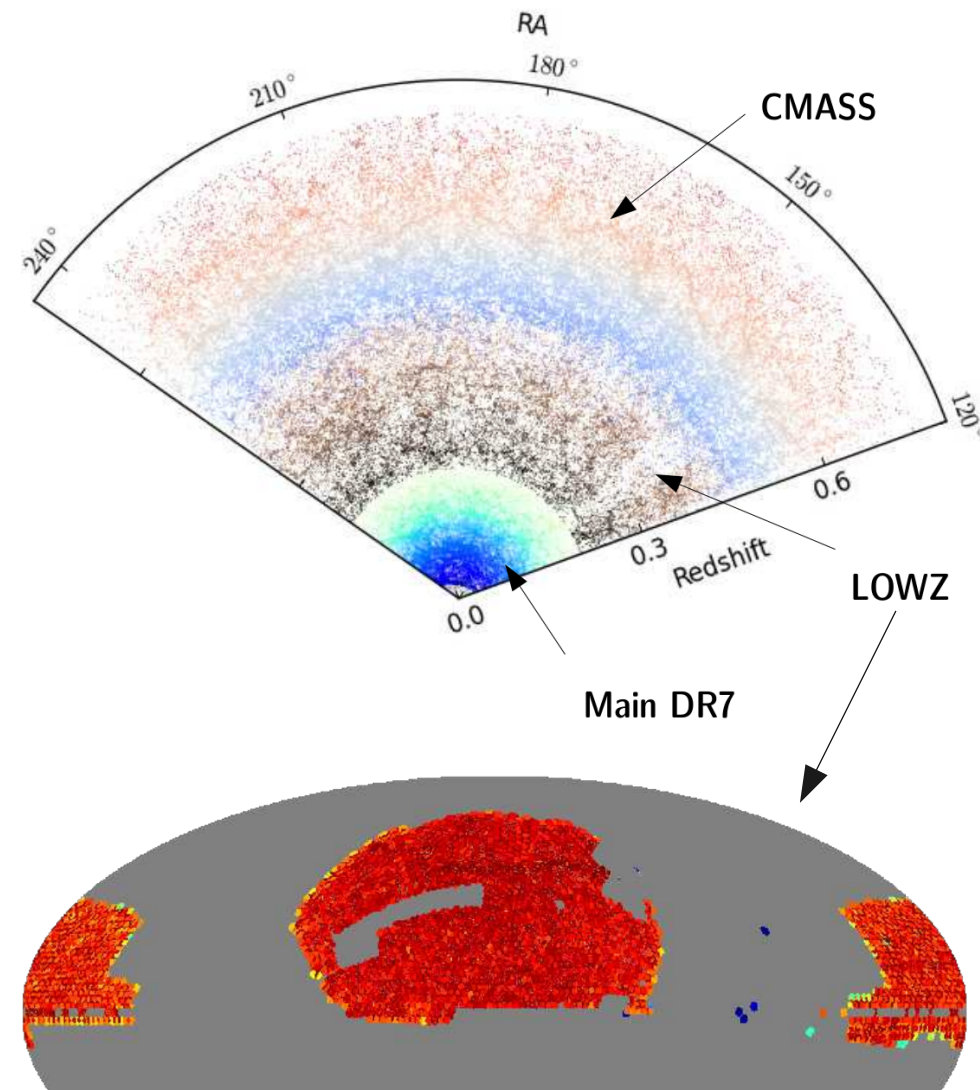
- Tested on low-resolution mock data
- Forward model: **LPT + AP**
- \sim Linear expansion regime
- Broad posterior for Ω_m

Validation on mock catalogues (B) - SDSSIII

Simulation box

Grid with 128^3 voxels
4000 Mpc side length

- Forward model: **LPT + AP**
- Highly structured survey geometry & selection effects



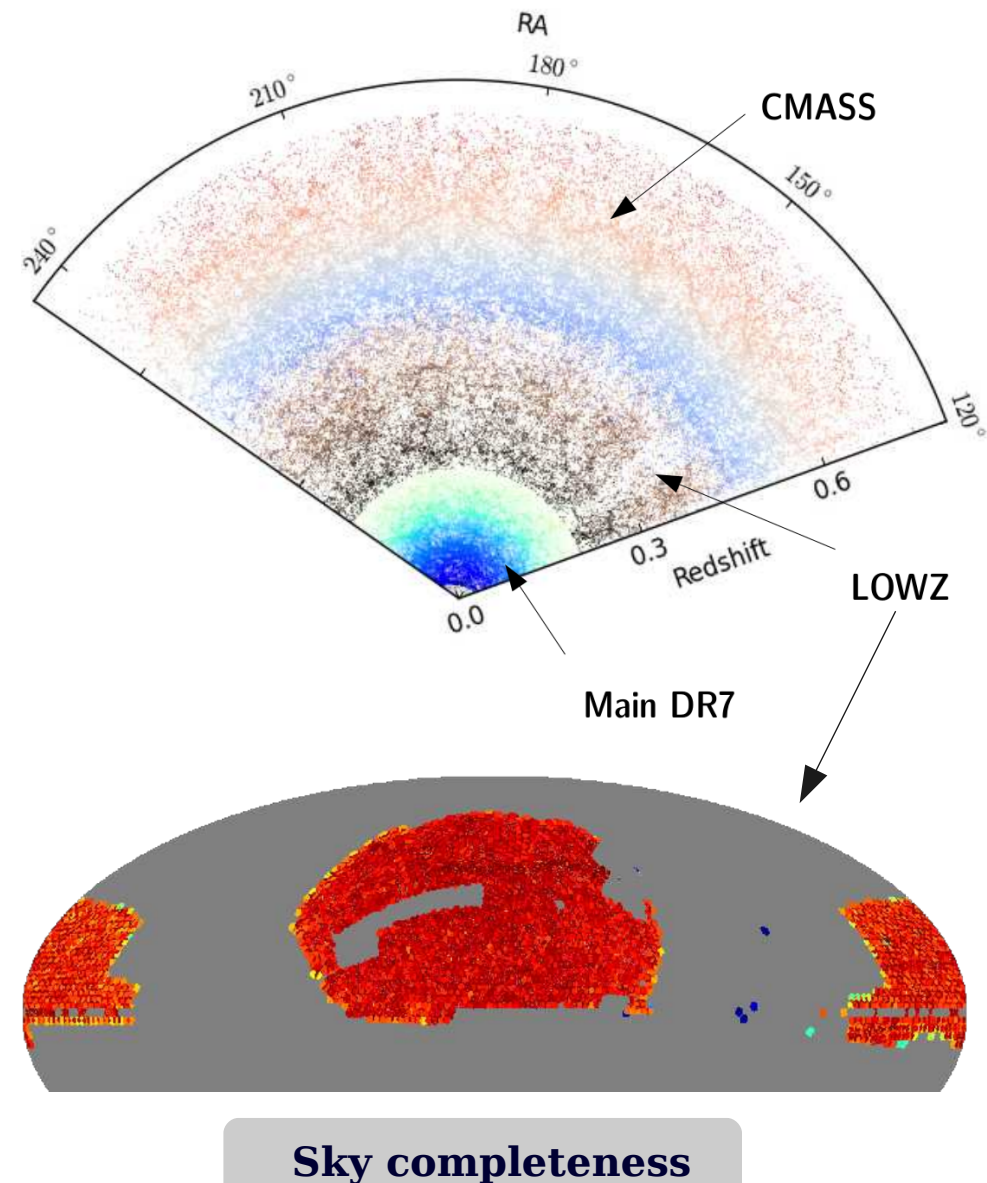
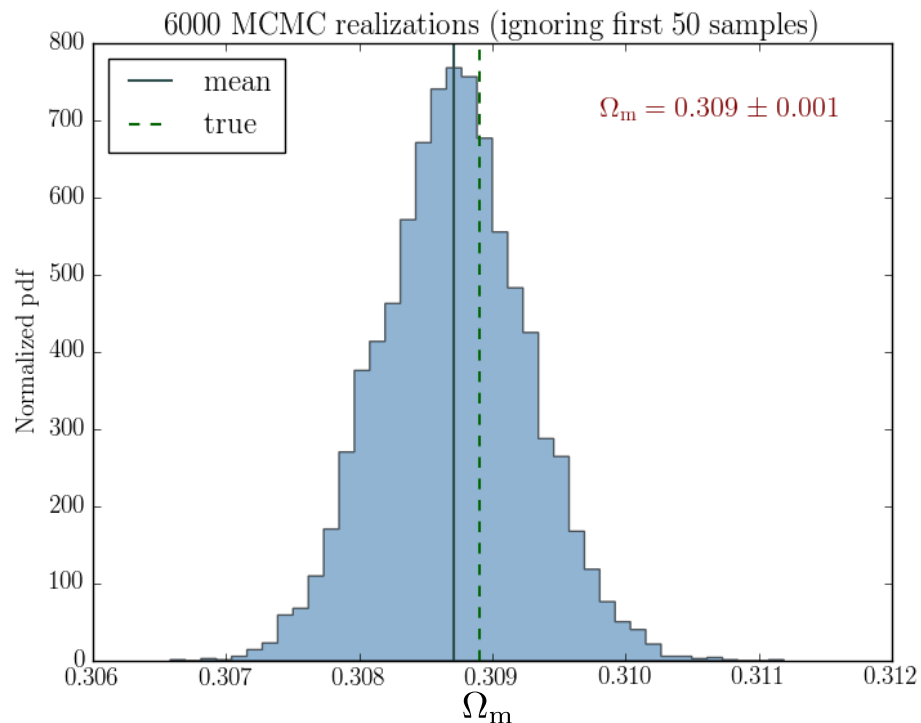
Sky completeness

Validation on mock catalogues (B) - SDSSIII

Simulation box

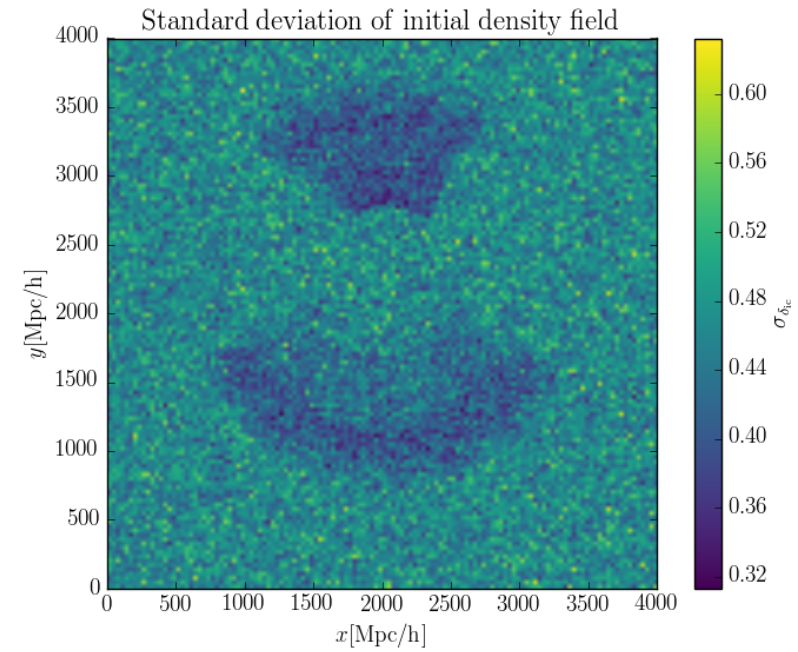
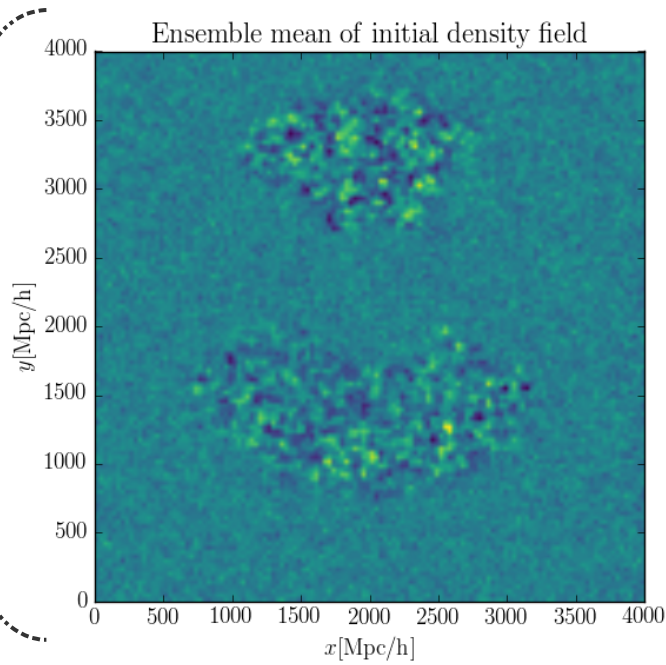
Grid with 128^3 voxels
4000 Mpc side length

- Forward model: **LPT + AP**
- Probing higher redshift range; AP distortion due to cosmic expansion is much more informative
- Tight constraints on Ω_m

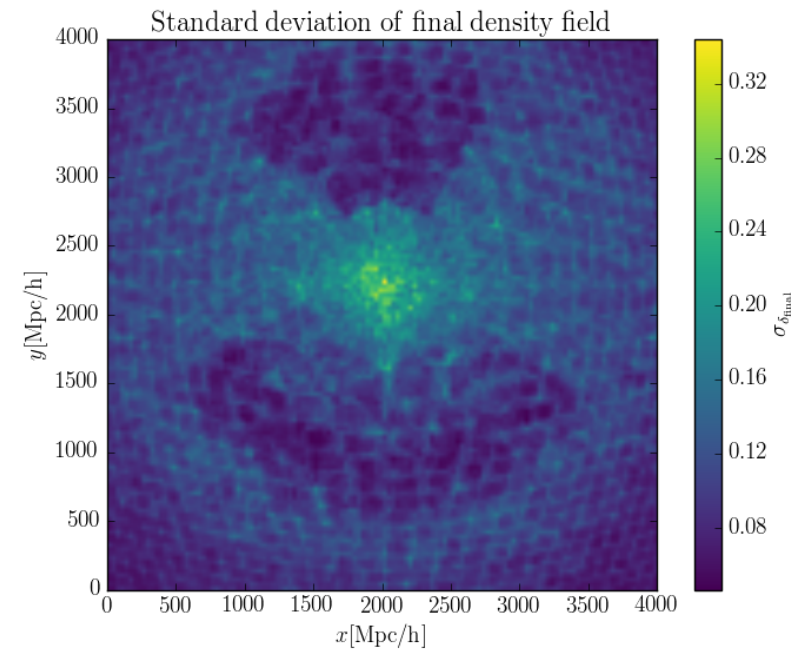
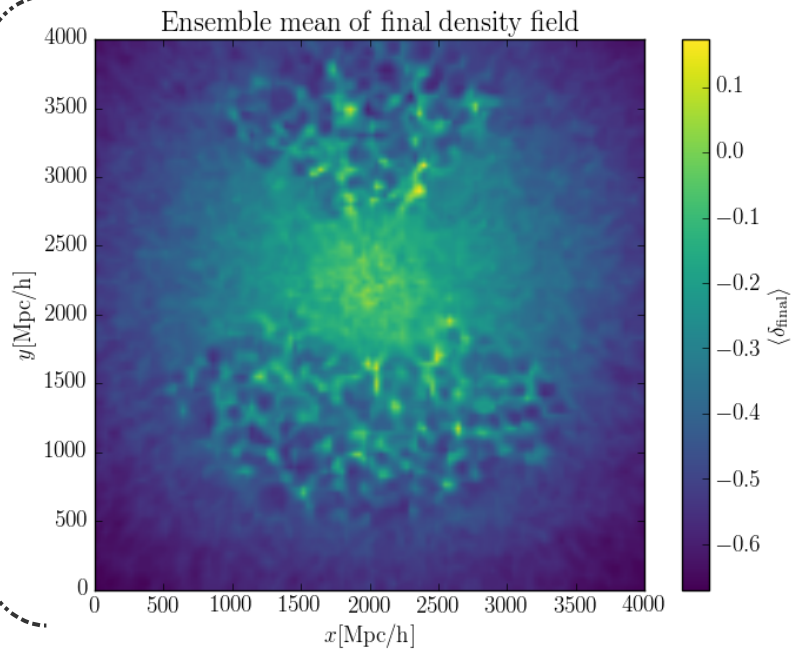


Ensemble mean & error maps

Initial density field



Slice through 3D density field



Final density field

Current & future work

Current project: (DKR, Lavaux & Wandelt 2018c, in prep.)

- ✓ Implemented forward model for **AP distortion** and cosmological parameter sampler
- ✓ Tested on low-resolution mock (2M++, SDSS-III) data
- ✓ Chain forward models: **LPT + AP**
 - Upgrade forward model to **2LPT** and jointly infer mean density of tracers & bias also
 - Assess impact of redshift space distortions (**RSDs**) on cosmological constraints

Current & future work

Current project: (DKR, Lavaux & Wandelt 2018c, in prep.)

- ✓ Implemented forward model for **AP distortion** and cosmological parameter sampler
- ✓ Tested on low-resolution mock (2M++, SDSS-III) data
- ✓ Chain forward models: **LPT + AP**
 - Upgrade forward model to **2LPT** and jointly infer mean density of tracers & bias also
 - Assess impact of redshift space distortions (**RSDs**) on cosmological constraints

Future work:

- Encode power spectrum inference in the block sampling scheme
- Account for **RSDs** in the data model
- Showcase application of **ALTAIR** on real data sets (e.g. **SDSS-III**):
 - Joint inference of 3D density field, underlying power spectrum & cosmological parameters

Follow-up project



Relevant for current & next-generation galaxy redshift surveys (Euclid, LSST, ...)